

MULTINODE ACTIVATION AND TERMINATION
METHOD AND SYSTEM

FIELD OF THE INVENTION

5 The present invention relates generally to electronic business technology, and more particularly, to business process automation and to a multinode activation and termination method and system.

10 BACKGROUND OF THE INVENTION

Workflow management is a rapidly evolving technology that many businesses in a variety of industries utilize to handle business processes. A business process, as defined by the Workflow standard - Terminology & glossary, Technical Report WPMC-TC-1011, Workflow Management Coalition, June 1996. Versions 2.0., is simply a set of one or more linked activities that collectively realize a business objective or a policy goal, typically within the context of an organizational structure defining functional roles and relationships. A workflow is defined as the automation of a business process, in whole or in part, during which documents, information, or activities are passed from one participant to another, according to a set of predefined rules. A workflow management system (WfMS) defines, creates, and manages the execution of workflows.

Examples of workflow software include BusinessWare software, available from Vitria Technology, Inc. of

Sunnyvale, California, Inconcert software, available from TIBCO Software, Inc. of Palo Alto, California, MQ Series software, available from International Business Machines Corporation (IBM), of Armonk, New York, and Staffware 2000, available from Staffware of Berkshire, United Kingdom.

There are hundreds of commercial workflow management systems (WfMSs), which are available on the market, as well as many research prototypes. While each system has a different process model, most of them share the same basic concepts. In one example, a process is described by a directed graph that has four different kinds of nodes.

Work nodes (also called service nodes) represent the invocation of activities (also called services), which are assigned for execution to a human or automated resource. Route nodes are decision points that route the execution flow among nodes based on an associated routing rule. Start nodes denote the entry point to the process. Typically, only one start node is allowed in a process. Complete nodes denote termination points.

There are many business processes in which an activity needs to be executed multiple times in parallel. For example, a restaurant brokering service may need to request the rates and availability from several restaurants that provide on-line access to this type of information. The request node that requests rates and availability may need to be repeated for all the restaurants that meet a particular criteria (e.g., in a particular vicinity).

In some of these applications, the exact number of activations for the node is known at the time when the process definition is created. For example, in a small town, the number of restaurants may be relatively static.

5 However, there are other applications where the exact number of parallel activations is not known at the time when the process definition is generated. For example, in a large metropolitan area, the number of restaurants may vary widely since many restaurants may open for business or
10 close for business on any given day.

To model such a business process with traditional process models, the process developer is required to employ very complex process definitions to attempt to account for all the possible cases. For example, the developer may
15 "guess" a maximum number of parallel activities that need to be activated in executions of the business process. In the example above, a process developer may assume that there will be at most twenty (20) restaurants. The developer then models a corresponding number of nodes in
20 the workflow definition. FIG. 7 illustrates an exemplary process definition that has a request node for each of the twenty restaurants. Unfortunately, these complex process definitions are difficult to specify and even more difficult to maintain. Furthermore, this approach is
25 limited since when there are more restaurants than the assumed maximum number (e.g., a number greater than twenty

in this case), there is no provision in the process definition to handle such a case.

Some prior art approaches allow the multiple activation of services for each node, where the number of instances is based on the number of available resources. 5 The Process Manager product available from Hewlett-Packard (HP) of Palo Alto, California, the assignee of the present invention, is an example of such an approach. In this approach, multiple activities can be executed in parallel 10 within a work node. However, it is noted that the number of activities that are executed in parallel is always equal to the number of resources that are available for execution of that activity. In other words, no other criteria for the selection of the number of parallel activations are 15 possible.

Furthermore, each activity is assigned to a different resource. Also, all the activities have the same input data. Moreover, the attributes of the node (e.g., the service selection, resource selection, security, exception 20 handling specification) are the same for every activity execution within the work node. As can be appreciated, such a solution lacks flexibility. In fact, it would instead be desirable to have different resource selection criteria, different data, and different security and 25 exception handling criteria depending on the purpose of the activity execution.

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Consequently, it would be desirable to have a mechanism that allows for multiple executions, where the input can be varied for each execution, and the attributes of the execution can be varied for each execution, thereby

5 providing a flexible solution.

Based on the foregoing, there remains a need for a multinode method and system having activation rules and termination rules that overcomes the disadvantages set forth previously.

SUMMARY OF THE INVENTION

According to one embodiment of the present invention, a method and system for processing workflows having at least one multinode (also referred to herein as a multi-
5 service node) is described.

One aspect of the present invention is the provision of resource-based multinode activation rules.

Another aspect of the present invention is the provision of variable-based multinode activation rules.

10 Another aspect of the present invention is the provision of multinode termination conditions, where all nodes in the multinode must complete processing before processing for the multinode is terminated.

15 Another aspect of the present invention is the provision of termination conditions where less than all the nodes need to complete processing before processing for the multinode is terminated.

20 According to one embodiment, a multinode activation and termination method and system is provided for allowing multiple parallel instances of a same node to be invoked. First, a multinode is defined that allows for multiple parallel activation of a work node. At run time, a determination is made of the number of work nodes to be activated based on an activation rule. The work nodes are
25 then executed. Each work node can be provided with different input data for execution, thereby allowing one to fine tune the input and attributes of each work node. A

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termination rule is utilized to determine when the execution of the multinode is completed. When the execution of the multinode is complete, a successor node is then executed. When the execution of the multinode is not
5 complete, processing continues within the multinode.

Other features and advantages of the present invention will be apparent from the detailed description that follows.

BRIEF DESCRIPTION OF THE DRAWINGS

The present invention is illustrated by way of example, and not by way of limitation, in the figures of the accompanying drawings and in which like reference
5 numerals refer to similar elements.

FIG. 1 illustrates an architecture for processing nodes according to one embodiment of the present invention can be utilized.

FIG. 2 is a block diagram of a multi-service node
10 mechanism according to one embodiment of the present invention.

FIG. 3 is a flow chart illustrating the processing steps related to multi-service node activation that are performed by the multi-service node mechanism of FIG. 2 in
15 accordance with one embodiment of the present invention.

FIG. 4 is a flow chart illustrating the processing steps related to multi-service node termination that are performed by the multi-service node mechanism of FIG. 2 in accordance with one embodiment of the present invention.

FIG. 5 is an exemplary restaurant reservation workflow in which the multinode activation by resource may be utilized and in which multinode termination in accordance with one embodiment of the present invention may be utilized.
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FIG. 6 is an exemplary travel reservation workflow in which the multinode activation by variable may be utilized and in which multinode termination in accordance with an
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alternative embodiment of the present invention may be utilized.

FIG. 7 illustrates an exemplary prior art process definition.

DETAILED DESCRIPTION OF THE INVENTION

A method and system for multinode activation and termination are described. In the following description, for the purposes of explanation, numerous specific details are set forth in order to provide a thorough understanding of the present invention. It will be apparent, however, to one skilled in the art that the present invention may be practiced without these specific details. In other instances, well-known structures and devices are shown in block diagram form in order to avoid unnecessarily obscuring the present invention.

Architecture 100

FIG. 1 illustrates an architecture 100 for processing multinodes according to one embodiment of the present invention. The architecture 100 includes a workflow engine 110 that can, for example, be an application that executes on a processor. The workflow engine 110 retrieves a process definition 114 (e.g., a flowchart). The workflow engine 110 then determines the first work node to execute. Next, the workflow engine 110 determines (e.g., reads) an activity corresponding to the first work node.

Then, the workflow engine 110 determines a resource rule corresponding to the activity. Preferably, the workflow engine 110 queries a resource executive 130 (e.g., the Process Manager product available from Hewlett-Packard (HP) of Palo Alto, California, the assignee of the present

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invention) to obtain a single resource or list of resources. An example of a single resource is the name of an individual in the organization, who is responsible for performing the activity. An example of a list of resources
5 is a list of names of individuals in the organization, who are responsible for performing the activity.

Once the workflow engine 110 receives the list of resources, the workflow engine 110 assigns the activity to a particular resource 134 (e.g., resourceA, ..., resourceN).
10 When the resource 134 completes the activity, the resource 134 notifies the workflow engine 110 of completion. The workflow engine 110 then retrieves the process definition 114 to determine the next node in the workflow for processing. The next work node is then processed in a
15 manner similar to the first work node. This process is repeated for all work nodes until the all nodes in the workflow are processed.

The workflow engine 110 can include a multinode mechanism 150 for processing multinodes. It is noted that
20 the multinode mechanism 150 is preferably implemented as part of the workflow engine 110 (e.g., incorporated in the workflow engine 110). Alternatively, the multinode mechanism 150 can be implemented as a module that is separate from the workflow engine 110. In this case, the
25 multinode mechanism 150 communicates with the workflow engine 110, but is not part of the workflow engine 110.

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The multinode mechanism 150 (also referred to herein as a multinode handling facility) handles activation of the multinode and termination of the multinode. In one embodiment, the multinode mechanism 150 determines the number of nodes in the multinode to be activated based on an activation rule, executes the nodes in the multinode; determines when the execution of the multinode is completed based on a termination rule, and when the execution of the multinode is complete, executing a successor node. The multinode mechanism 150 is described in greater detail hereinafter with reference to FIG. 2.

Multinode Mechanism 150

FIG. 2 is a block diagram of a multinode mechanism 150 according to one embodiment of the present invention. The multinode mechanism 150 includes a multinode determination unit (MDU) 210 for receiving a node definition 214 and determining whether the current node is a normal work node or a multinode. The multinode mechanism 150 also includes an activation facility 220 for receiving an activation rule 224 and based thereon for determining whether activation is by resource (resource-based activation) or by variable (variable-based activation).

The multinode mechanism 150 also includes a resource-based activation facility 240 for processing activation by resource and a variable-based activation facility 250 for processing activation by variable.

The resource-based activation facility 240 includes a resource rule execution unit (RREU) 244 for executing the resource rule of the multinode. For example, the resource rule may be specified in a service node tag of the multinode description. The resource-based activation facility 240 further includes a new instance generation unit (NIGU) 248 for starting new instances of the multinode for each new resource in the resource list.

The variable-based activation facility 250 includes a variable name reader 254 for reading the variable name V. For example, variable V may be of type vector or list. The variable-based activation facility 250 further includes a new instance generation unit (NIGU) 258 for starting new instances of the multinode for each new element in the vector or list identified by the variable name.

Multi-Service Node Activation Processing

FIG. 3 is a flow chart illustrating the processing steps related to multi-service node activation that are performed by the multi-service node mechanism of FIG. 2 in accordance with one embodiment of the present invention. In step 310, a new node is scheduled for execution by the workflow engine 110. In step 320, the workflow engine 110 reads the node definition. In decision block 330, a determination is made based on the node definition whether the current node is a multi-service node or a non-multi-service node.

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When the current node is a multi-service node, processing proceeds to processing step 340. When the current node is not a multi-service node, processing proceeds to processing step 334, where normal node
5 activation occurs. Normal node activation procedure is well-known to those of ordinary skill in the art and is not discussed further herein.

In step 340, the workflow engine 110 reads the activation rule. The activation rule can, for example, be
10 specified by an activation tag in a mark-up language (e.g., XML) service description. In decision block 350, a determination is made whether the activation is by resource (i.e., resource-based activation) or by variable (i.e., variable-based activation).

15 In step 360, the workflow engine 110 executes the resource rule of the service node as specified in the SERVICE_NODE tag of the multi-service description. In step 364, the workflow engine 110 starts a new instance of the service node as specified in the SERVICE_NODE tag of the
20 multi-service description. The new instance is assigned to the current resource. In decision block 368, a determination is made whether there are more resources to which a new instance of a service node should be assigned. In other words, the decision block determines whether all
25 resources have been processed. When all resources have been processed, processing ends. When there are more resources to be processed, processing proceeds to step 364.

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It is noted that steps 364 and 368 are repeated for each resource **r** returned by the resource rule execution. Hence, in this case the number of service nodes activated is equal to the number of available resources for executing the
5 node.

In step 370, the workflow engine 110 reads the variable name **V**. The variable name **V** can be, for example, of type vector or list. In step 374, the workflow engine 110 starts a new instance of the service node as specified
10 in the SERVICE_NODE tag of the multi-service description. The value contained in the position **i** of vector **V** is passed as an input parameter to the service node.

In decision block 378, a determination is made whether there are more elements in vector **V** to be processed. In
15 other words, the decision block determines whether all elements in vector **V** have been processed. When all elements in vector **V** have been processed, the processing ends. When there are more elements to be processed, processing proceeds to step 374. It is noted that steps
20 374 and 378 are repeated for each element **i** in vector **V**.

Multi-Service Node Termination Processing

FIG. 4 is a flow chart illustrating the processing steps related to multi-service node termination that are
25 performed by the multi-service node mechanism of FIG. 2 in accordance with one embodiment of the present invention. In step 410, the execution of a node is completed. In step

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420, the workflow engine 110 reads a definition of the completed node. In decision block 430, a determination is made whether the node is part of a multi-service node.

When the current node is part of a multi-service node, processing proceeds to processing step 440. When the current node is not part of a multi-service node, processing proceeds to processing step 450, where normal node termination occurs. Normal node termination procedure is well-known to those of ordinary skill in the art and is not discussed further herein.

In step 440, the workflow engine 110 evaluates the termination condition that is specified in the TERMINATION tag. In decision block 460, a determination is made whether the termination condition is true. When the termination condition is true, in step 470, the multi-service node is completed. Otherwise, when the termination condition is false, the multi-service node is not completed, and processing ends (i.e., the multiservice node continues to execute).

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Exemplary Restaurant Reservation Workflow

FIG. 5 is an exemplary restaurant reservation workflow 500 in which multinode activation by resource may be utilized and in which multinode termination in accordance with one embodiment of the present invention may be utilized. The process definition 500 has a start node 510 (e.g., StartNode2), a first work node 520 (e.g.,

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ProcessCustomerRegeust2) that processes the customer request, a multinode 530 (e.g., RestaurantRateRequest), a second work node 540 (e.g., NotifyCustomer2) that notifies the customer of the rates of the different restaurants, and
5 a complete node 550(e.g., CompleteNode2).

In this restaurant reservation workflow 500, all available restaurants need to be contacted for price information. It is noted that the restaurants are considered to be resources in this example. Accordingly,
10 the multinode 530 may be activated by resource (steps 360-368 of FIG. 3).

It is further noted that termination for multinode 530 can be based upon the condition that information from all the restaurants has been received. In other words, the
15 multinode 530 terminates when all work nodes in the multinode 530 have been completed according to one embodiment of the present invention.

Exemplary Travel Reservation Workflow

20 FIG. 6 is an exemplary travel reservation workflow 600 in which multinode activation by variable of the present invention may be utilized and in which multinode termination in accordance with an alternative embodiment of the present invention may be utilized.

25 The process definition 600 has a start node 610 (e.g., StartNode3), a first work node 620 (e.g., FlightHotelAvailability) that checks flight availability

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and hotel availability, a multinode 630 (e.g., RequestVisa), a route node 640 (e.g., RouteNode5), a work node 650 (e.g., BookTravel), a complete node 660 (e.g., CompleteNode3), and a complete node 670 (e.g., CompleteNode4). The route node 640 routes processing to the work node 650 (e.g., BookTravel) when all the visas are granted. The route node 640 routes processing to the complete node 670 (e.g., CompleteNode4) when some of the visas are not granted.

10 The multinode 630 is employed to request a visa for all tourists in a group. Accordingly, activation of the multinode 630 may be accomplished by variable since the request for visas depends on the number of tourists in the group. It is noted that the consulates that release visas
15 to the tourists are considered to be the resources in this case. The activation cannot be based on the number of resources (i.e., consulates), since there is no correlation between the number of tourists that need visas and the number of available resources (i.e., consulates that can
20 release visas). Instead, a variable in the workflow instance can be utilized to indicate the number of visas that need to be requested in accordance with the present invention.

With this workflow, a multinode termination condition
25 in accordance with an alternative embodiment of the present invention may be utilized. For example, workflow execution can proceed from the multinode 630 to the route node 640

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when either all the visas have been received or when at least one visa has been declined. This example illustrates a case where the multinode may be terminated even before all work nodes have been completed.

5 In the foregoing specification, the invention has been described with reference to specific embodiments thereof. It will, however, be evident that various modifications and changes may be made thereto without departing from the broader scope of the invention. The specification and
10 drawings are, accordingly, to be regarded in an illustrative rather than a restrictive sense.

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